## LOWER KEY STAGE 2

In Lower Key Stage 2, children build on the concrete and conceptual understandings they have gained in Key Stage 1 to develop a real mathematical understanding of the four operations, in particular developing arithmetical competence in relation to larger numbers.

## Addition and subtraction: Children are taught to use place value

 and number facts to add and subtract numbers mentally and they will develop a range of strategies to enable them to discard the 'counting in 1s' or fingers-based methods of Key Stage 1. In particular, children will learn to add and subtract multiples and near multiples of 10,100 and 1000, and will become fluent in complementary addition as an accurate means of achieving fast and accurate answers to 3-digit subtractions. Standard written methods for adding larger numbers are taught, learned and consolidated, and written column subtraction is also introduced.Multiplication and division: This key stage is also the period during which all the multiplication and division facts are thoroughly memorised, including all facts up to $12 \times 12$. Efficient written methods for multiplying or dividing a 2-digit or 3-digit number by a 1-digit number are taught, as are mental strategies for multiplication or division with large but 'friendly' numbers, e.g. when dividing by 5 or multiplying by | 20. |
| :--- |

Fractions and decimals: Children will develop their understanding of fractions, learning to reduce a fraction to its simplest form, as well as finding non-unit fractions of amounts and quantities. The concept of a decimal number is introduced and children consolidate a firm understanding of 1-place decimals, multiplying and dividing whole numbers by 10 and 100.

## Year 3 Mental Methods

## Using place value

Count in 100s
e.g. Know $475+200$ as $475,575,675$


Add multiples of 10, 100 and $£ 1$
e.g. $746+200$
e.g. $746+40$
e.g. $£ 6 \cdot 34+£ 5$ as $£ 6+£ 5$ and 34 p

Partitioning
e.g. $£ 8 \cdot 50+£ 3 \cdot 70$ as $£ 8+£ 3$ and 50 p +70 p and combine the totals: $£ 11+£ 1 \cdot 20$
e.g. $347+36$ as 300 and $40+30$ and $7+6$ and combine the totals: $370+13=383$
e.g. $68+74$ as $60+70$ and $8+4$ and combine
the totals: $130+12=142$


## Year 3 Written Methods

Build on partitioning to develop expanded column addition with two 3-digit numbers
e.g. $466+358$

$$
\begin{array}{r}
40060 \quad 6 \\
+\quad 30050 \quad 8 \\
\hline 700110 \quad 14=824
\end{array}
$$

Use expanded column addition where digits in a column add to more than the column value
e.g. $466+358$

$$
\begin{array}{r}
400 \\
300 \\
50 \\
\hline
\end{array}
$$

Compact column addition with two or more 3-digit numbers or towers of 2-digit numbers
e.g. $347+286+495$

$$
\begin{array}{r}
347 \\
286 \\
+\quad 495 \\
21 \\
\hline 1128 \\
\hline
\end{array}
$$

Compact column addition with 3 - and 4 -digit numbers Recognise like fractions that add to 1

$$
\begin{aligned}
& \text { e.g. } 1 / 4+3 / 4 \\
& \text { e.g. } 3 / 5+2 / 5
\end{aligned}
$$

## Counting on

Add two 2-digit numbers by adding the multiple of 10 , then the 1 s e.g. $67+55$ as $67+50(117)+5=122$

Add near multiples of 10 and 100
e.g. $67+39$
e.g. $364+199$

Add pairs of 'friendly' 3 -digit numbers
e.g. $548+120$

Count on from 3-digit numbers
e.g. $247+34$ as $247+30(277)+4=281$

Using number facts
Know pairs which total each number to 20
e.g. $7+8=15$
e.g. $12+6=18$

Number bonds to 100
e.g. $35+65$
e.g. $46+54$
e.g. $73+27$
$0000000000000000000000000000000000-00000000000000000000000000000000000000000000000000000000000000000$
Add to the next 10 and the next 100
e.g. $176+4=180$
e.g. $435+65=500$


## Year 3 Mental Methods

Count back in $100 \mathrm{~s}, 10$ s then 1 s
e.g. $763-121$ as $763-100$ (663) $-20(643)-1=642$


Subtract near multiples of 10 and 100
e.g. 648-199
e.g. 86-39

## Counting up

Find a difference between two numbers by counting up from the smaller to the larger
e.g. 121-87


Year 3 Written Methods
Use counting up subtraction to find change from £1, £5 and £10 e.g. £10.00-£6.84


Recognise complements of any fraction to 1
e.g. $1-1 / 4=3 / 4$
e.g. $1-3 / 5=2 / 5$

## Year 3 Mental Methods

Year 3 Written Methods
Using number facts
Know pairs which total each number to 20
e.g. $20-14=6$

Number bonds to 100
e.g. $100-48=52$
e.g. $100-35=65$
$0000000000000000000000000000000000000000000000000000000000000000-000000000000000000000000000000000$

Subtract using number facts to bridge back through a 10
e.g. $42-5=42-2(40)-3=37$

## Year 3 Mental Methods

## Counting in steps ('clever' counting)

Count in $2 \mathrm{~s}, 3 \mathrm{~s}, 4 \mathrm{~s}, 5 \mathrm{~s}, 8 \mathrm{~s}$ and 10 s

Multiplication

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |



Year 3 Written Methods

Build on partitioning to develop grid multiplication e.g. $23 \times 4$

| $\times$ | 20 | 3 |
| ---: | ---: | ---: |
| 4 | 80 | 12 |$=92$

Year 3 Mental Methods
Year 3 Written Methods

## Doubling and halving

Find doubles of numbers to 50 using partitioning e.g. double 48


Use doubling as a strategy in multiplying by 2
e.g. $18 \times 2$ is double $18=36$

## Grouping

Recognise that multiplication is commutative
e.g. $4 \times 8=8 \times 4$

Multiply multiples of 10 by 1 -digit numbers
e.g. $30 \times 8=240$

Multiply 'friendly' 2 -digit numbers by 1 -digit numbers e.g. $13 \times 4$

Using number facts
Know doubles to double 20
e.g. double 15 is 30

Know doubles of multiples of 5 to 100
e.g. double 85 is 170

Know $\times 2, \times 3, \times 4, \times 5, \times 8, \times 10$ tables facts

## Year 3 Mental Methods

## Counting in steps ('clever’ counting)

Count in $2 \mathrm{~s}, 3 \mathrm{~s}, 4 \mathrm{~s}, 5 \mathrm{~s}, 8 \mathrm{~s}$ and 10 s

Division

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |



## Year 3 Written Methods

## Using number facts

Know half of even numbers to 40
Know half of multiples of 10 to 200
e.g. half of 170 is 85

Know $\times 2, \times 3, \times 4, \times 5, \times 8, \times 10$ division facts

Perform divisions just above the 10th multiple using written jottings, understanding how to give a remainder as a whole number
Use division facts to find unit and simple non-unit fractions of amounts within the times-tables
e.g. $3 / 4$ of 48 is $3 \times(48 \div 4)=36$

## Year 3 Mental Methods

Year 3 Written Methods

## Doubling and halving

Find half of even numbers to 100 using partitioning e.g. find half of 48


Use halving as a strategy in dividing by 2
e.g. $36 \div 2$ is half of $36=18$

Find half of odd numbers

Year 3 Mental Methods
Year 3 Written Methods

## Grouping

Recognise that division is not commutative
e.g. $16 \div 8$ does not equal $8 \div 16$

Relate division to multiplications 'with holes in'
e.g. _ $\times 5=30$ is the same calculation as $30 \div 5=$ _ thus we can count in 5s to find the answer


Divide multiples of 10 by 1 -digit numbers
e.g. $240 \div 8=30$

Begin to use subtraction of multiples of 10 of the divisor to divide numbers above the 10th multiple
e.g. $52 \div 4$ is $10 \times 4(40)$ and $3 \times 4(12)=13$

